Showing Triangles are Similar: SSS and SAS

## Goal

Show that two triangles are similar using the SSS and SAS Similarity Theorems.

## **Key Words**

• similar polygons p. 365

The triangles in the Navajo rug look similar. To show that they are similar, you can use the definition of similar polygons or the AA Similarity Postulate.

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In this lesson, you will learn two new methods to show that two triangles are similar.



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### THEOREM 7.2



Words If the corresponding sides of two triangles are proportional, then the triangles are similar.

**Symbols** If  $\frac{FG}{AB} = \frac{GH}{BC} = \frac{HF}{CA}$ , then  $\triangle ABC \sim \triangle FGH$ .

## EXAMPLE 1 Use the SSS Similarity Theorem

Determine whether the triangles are similar. If they are similar, write a similarity statement and find the scale factor of Triangle B to Triangle A.



### **Solution**

Find the ratios of the corresponding sides.

$$\frac{SU}{PR} = \frac{6}{12} = \frac{6 \div 6}{12 \div 6} = \frac{1}{2}$$
$$\frac{UT}{RQ} = \frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$
$$\frac{TS}{QP} = \frac{4}{8} = \frac{4 \div 4}{8 \div 4} = \frac{1}{2}$$

All three ratios are equal. So, the corresponding sides of the triangles are proportional.

ANSWER By the SSS Similarity Theorem,  $\triangle PQR \sim \triangle STU$ . The scale factor of Triangle B to Triangle A is  $\frac{1}{2}$ .



# Checkpoint V Use the SSS Similarity Theorem

Determine whether the triangles are similar. If they are similar, write a similarity statement.





### Student Help

STUDY TIP

When using the SSS Similarity Theorem, compare the shortest sides, the longest sides, and then the remaining sides. .....

#### 3 Use the SAS Similarity Theorem EXAMPLE

Determine whether the triangles are similar. If they are similar, write a similarity statement.



### Solution

 $\angle C$  and  $\angle F$  both measure 61°, so  $\angle C \cong \angle F$ .

Compare the ratios of the side lengths that include  $\angle C$  and  $\angle F$ .

Shorter sides  $\frac{DF}{AC} = \frac{5}{3}$  Longer sides  $\frac{FE}{CB} = \frac{10}{6} = \frac{5}{3}$ 

The lengths of the sides that include  $\angle C$  and  $\angle F$  are proportional.

**ANSWER** By the SAS Similarity Theorem,  $\triangle ABC \sim \triangle DEF$ .

#### 4 Similarity in Overlapping Triangles **EXAMPLE**

Show that  $\triangle VYZ \sim \triangle VWX$ .

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## Student Help

**VISUAL STRATEGY** Redraw overlapping triangles as two separate triangles, as shown on p. 356.

**Solution** 

Separate the triangles,  $\triangle VYZ$  and  $\triangle VWX$ , and label the side lengths.



 $\angle V \cong \angle V$  by the Reflexive Property of Congruence.

**Shorter sides** 

 $\frac{VW}{VY} = \frac{4}{4+8} = \frac{4}{12} = \frac{1}{3} \qquad \qquad \frac{XV}{ZV} = \frac{5}{5+10} = \frac{5}{15} = \frac{1}{3}$ 

Longer sides

The lengths of the sides that include  $\angle V$  are proportional.

**ANSWER** By the SAS Similarity Theorem,  $\triangle VYZ \sim \triangle VWX$ .

Checkpoint V **Use the SAS Similarity Theorem** 

> Determine whether the triangles are similar. If they are similar, write a similarity statement. Explain your reasoning.



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# **Guided Practice**

- **Vocabulary Check**
- **1.** If two sides of a triangle are proportional to two sides of another triangle, can you conclude that the triangles are similar?

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## Skill Check

In Exercises 2 and 3, determine whether the triangles are similar. If they are similar, write a similarity statement.



**4.** Is either  $\triangle LMN$  or  $\triangle XYZ$  similar to  $\triangle ABC$ ? Explain.



# **Practice and Applications**

### **Extra Practice**

See p. 688.

**SSS Similarity Theorem** Determine whether the two triangles are similar. If they are similar, write a similarity statement and find the scale factor of Triangle B to Triangle A.



## Homework Help

Example 1:	Exs. 5–10, 21–26
Example 2: Example 3:	Exs. 11–13 Exs. 14–18,
Example 4:	21–26 Exs. 19, 20, 26–29

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**14. A-Frame Building** Suppose you are constructing an A-frame home that is modeled after a ski lodge. The ski lodge and home are shown below. Are the triangles similar? Explain your reasoning.



**SAS Similarity Theorem** Determine whether the two triangles are similar. If they are similar, write a similarity statement.





### **HOMEWORK HELP** Extra help with problem solving in Exs. 15–18 is

solving in Exs. 15–18 is at classzone.com



**Overlapping Triangles** Show that the overlapping triangles are similar. Then write a similarity statement.





**Determining Similarity** Determine whether the triangles are similar. If they are similar, state the similarity and the postulate or theorem that justifies your answer.





- Shuffleboard In the portion of a shuffleboard
- 27. What piece of information do you need in order to show that  $\triangle ADE \sim \triangle ABC$ using the SSS Similarity Theorem?
- **28.** What piece of information do you need in order to show that  $\triangle ADE \sim \triangle ABC$ using the SAS Similarity Theorem?
- **29. You be the Judge** Jon claims that  $\triangle$  *SUV* is similar to  $\triangle$  *SRT* when *x* = 6. Dave believes that the triangles are similar when x = 5. Who is right? Explain your reasoning.







Link

SHUFFLEBOARD is played on a long flat court. Players earn points by using sticks called *cues* to push circular disks onto a scoring area at the opposite end of the court.

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